# MA281: Introduction to Linear Algebra 

## Baker University - Fall 2023

Unless otherwise noted, each of the following sections comes from the textbook Linear Algebra (Third Edition) by John B. Fraleigh and Raymond A. Beauregard.

## Exam 1: Vectors and Matrices

| date | day | section | topic(s) |
| :---: | :---: | :---: | :---: |
| $8 / 23$ | W | §1.1: Vectors in Euclidean Space | $\circ$ vector notation <br> $\circ$ vector algebra <br> $\circ$ properties of vectors |
| $8 / 25$ | F | §1.2: The Norm and the Dot Product | $\circ$ vector magnitude <br> $\circ$ unit vectors <br> $\circ$ vector dot product <br> $\circ$ angles between vectors |


| date | day | section | topic(s) |
| :---: | :---: | :---: | :---: |
| $8 / 28$ | M | §1.3: Matrices and Their Algebra | $\circ$ matrix addition <br> $\circ$ matrix multiplication <br> $\circ$ scalar multiplication <br> $\circ$ matrix transposition |
| $8 / 29$ | Tu | §1.4: Solving Systems of Linear Equations | $\circ$ elementary row operations <br> $\circ$ row-echelon form <br> o reduced row-echelon form <br> ○ Gaussian Elimination |
| $8 / 30$ | W | §1.4: Solving Systems of Linear Equations | $\circ$ elementary matrices <br> $\circ$ row equivalence |
| $9 / 1$ | F | §1.5: Inverses of Square Matrices | $\circ$ invertible matrices <br> $\circ$ computation of inverses |


| date | day | section | topic(s) |
| :---: | :---: | :---: | :---: |
| $9 / 4$ | M | Labor Day |  |
| $9 / 5$ | Tu | §1.6: Homogeneous Systems, etc. | ० vector subspaces <br> o span and linear combinations <br> ० basis of a vector space |
| $9 / 6$ | W | §1.6: Homogeneous Systems, etc. | ० row space of a matrix <br> o column space of a matrix <br> ० null space of a matrix |
| $9 / 8$ | F | §2.1: Independence and Dimension | ० span <br> o linear independence <br> ० determination of bases |


| date | day | section | topic(s) |
| :---: | :---: | :---: | :---: |
| $9 / 11$ | M | §2.2: The Rank of a Matrix | ० row rank <br> o column rank <br> o Rank-Nullity Theorem |
| $9 / 12$ | Tu | §4.1: Areas, Volumes, and Cross Products | ० determinants <br> o area of a parallelogram <br> o the vector cross product |
| $9 / 13$ | W | §4.1: Areas, Volumes, and Cross Products | ० volume of a box <br> o properties of cross product |
| $9 / 15$ | F | §4.2: The Determinant of a Square Matrix | o determinants <br> o minors of a matrix <br> o cofactors of a matrix <br> o adjugate of a matrix |


| date | day | section | topic(s) |
| :---: | :---: | :---: | :---: |
| $9 / 18$ | M | §4.3: Computations of Determinants, etc. | ० properties of determinants <br> o computing determinants |
| $9 / 19$ | Tu | §4.3: Computations of Determinants, etc. | o computing the adjugate <br> o computing matrix inverses |
| $9 / 20$ | W | Exam I Review |  |
| $9 / 22$ | F | Exam I Review |  |


| date | day | section | topic(s) |
| :---: | :---: | :---: | :---: |
| $9 / 25$ | M | Exam I Review |  |
| $9 / 26$ | Tu | Exam I |  |

## Exam 2: Eigenvalues, Eigenvectors, and Canonical Forms

| date | day | section | topic(s) |
| :---: | :---: | :---: | :---: |
| $9 / 27$ | W | Characteristic and Minimal Polynomials | $\circ$ characteristic matrix <br> $\circ$ characteristic polynomial <br> $\circ$ minimal polynomial |
| $9 / 29$ | F | Characteristic and Minimal Polynomials | $\circ$ computing the polynomials <br> $\circ$ relating the polynomials |


| date | day | section | topic(s) |
| :---: | :---: | :---: | :---: |
| $10 / 2$ | M | §5.1: Eigenvalues and Eigenvectors | $\circ$ properties of eigenvalues <br> $\circ$ computing eigenvalues |
| $10 / 3$ | Tu | §5.1: Eigenvalues and Eigenvectors | $\circ$ properties of eigenvectors <br> $\circ$ computing eigenvectors |
| $10 / 4$ | W | §5.2: Diagonalization | $\circ$ diagonalizability <br> $\circ$ form of a diagonalizable matrix |
| $10 / 6$ | F | §5.2: Diagonalization | $\circ$ orthogonal matrices <br> $\circ$ orthonormal matrices |


| date | day | section | topic(s) |
| :---: | :---: | :---: | :---: |
| $10 / 9$ | M | The Cayley-Hamilton Theorem | ० the characteristic polynomial <br> o the minimal polynomial <br> o a proof of Cayley-Hamilton |
| $10 / 10$ | Tu | The Smith Normal Form | o the characteristic matrix <br> ocomputing the Smith Normal Form |
| $10 / 11$ | W | The Smith Normal Form | $\circ$ elementary divisors <br> o invariant factors |
| $10 / 13$ | F | Fall Break |  |


| date | day | section | topic(s) |
| :---: | :---: | :---: | :---: |
| $10 / 16$ | M | The Rational Canonical Form | $\circ$ invariant factors <br> $\circ$ companion matrices |
| $10 / 17$ | Tu | The Rational Canonical Form | $\circ$ computing Rational Canonical Form |
| $10 / 18$ | W | The Jordan Canonical Form | $\circ$ elementary divisors <br> $\circ$ Jordan blocks |
| $10 / 20$ | F | The Jordan Canonical Form | $\circ$ computing Jordan Canonical Form |


| date | day | section | topic(s) |
| :---: | :---: | :---: | :---: |
| $10 / 23$ | M | Review of Canonical Forms | o diagonalizability <br> o diagonal matrices <br> o block-diagonal matrices |
| $10 / 24$ | Tu | Review of Canonical Forms | $\circ$ Smith Normal Form <br> $\circ$ invariant factors <br> $\circ$ elementary divisors <br> o Rational Canonical Form <br> $\circ$ Jordan Canonical Form |
| $10 / 25$ | W | Exam II Review |  |
| $10 / 27$ | F | Exam II Review |  |


| date | day | section | topic(s) |
| :---: | :---: | :---: | :---: |
| $10 / 30$ | M | Exam II Review |  |
| $10 / 31$ | Tu | Exam II |  |

## Exam 3: Vector Spaces and Linear Transformations

| date | day | section | topic(s) |
| :---: | :---: | :---: | :---: |
| $11 / 1$ | W | §2.3: Linear Transformations of Euclidean Spaces | ० functions <br> $\circ$ linearity <br> $\circ$ properties <br> $\circ$ subspaces |
| $11 / 3$ | F | §2.3: Linear Transformations of Euclidean Spaces | $\circ$ rank and nullity <br> $\circ$ matrices <br> $\circ$ invertibility |


| date | day | section | topic(s) |
| :---: | :---: | :---: | :---: |
| $11 / 6$ | M | §3.1: Vector Spaces | $\circ$ vector space definition <br> $\circ$ vector space examples |
| $11 / 7$ | Tu | $\S 3.1:$ Vector Spaces | $\circ$ vector space properties <br> o vector subspaces |
| $11 / 8$ | W | §3.2: Basic Concepts of Vector Spaces | $\circ$ span <br> $\circ$ linear independence <br> o subspace tests <br> $\circ$ vector space dimension |
| $11 / 10$ | F | §3.3: Coordinatization of Vector Spaces | $\circ$ ordered bases <br> $\circ$ coordinate vectors |


| date | day | section | topic(s) |
| :---: | :---: | :---: | :---: |
| 11/13 | M | §7.2: Matrix Representations and Similarity | - matrix representation o similarity of matrices - change of basis |
| 11/14 | Tu | §3.4: Linear Transformations | - properties <br> - injectivity <br> - surjectivity <br> - subspaces <br> - further examples |
| 11/15 | W | §3.5: Inner Product Spaces | - Vector Dot Product <br> - Matrix Dot Product <br> - further examples |
| 11/17 | F | §3.5: Inner Product Spaces | - properties <br> - Triangle Inequality <br> - Cauchy-Schwarz |


| date | day | section | topic(s) |
| :---: | :---: | :---: | :---: |
| $11 / 20$ | M | Exam III Review |  |
| $11 / 21$ | Tu | Exam III Review |  |
| $11 / 22$ | W | Thanksgiving Break |  |
| $11 / 24$ | F | Thanksgiving Break |  |


| date | day | section | topic(s) |
| :---: | :---: | :---: | :---: |
| $11 / 27$ | M | Exam III Review |  |
| $11 / 28$ | Tu | Exam III |  |

## Final Exam Review

| date | day | section | topic(s) |
| :---: | :---: | :---: | :---: |
| $11 / 29$ | W | Final Exam Review |  |
| $12 / 1$ | F | Final Exam Review |  |


| date | day | section | topic(s) |
| :---: | :---: | :---: | :---: |
| $12 / 4$ | M | Final Exam Review |  |
| $12 / 5$ | Tu | Final Exam Review |  |
| $12 / 6$ | W | Final Exam Review |  |
| $12 / 8$ | F | Final Exam Review |  |

Final Exam: Monday, December 11 from 3:00 to 6:00 PM in Mulvane 409

